

1. Calculate the e-values of the Hamiltonian matrix describing two state system of decaying kaons. Hint: use the partially finished calculation shown during the lecture.
2. Check by direct substitution that the following time dependent states:

$$|K_S^0(t)\rangle = e^{-\frac{i}{\hbar}(m_S - \frac{i}{2}\gamma_S)t} |K_S^0\rangle$$

$$|K_L^0(t)\rangle = e^{-\frac{i}{\hbar}(m_L - \frac{i}{2}\gamma_L)t} |K_L^0\rangle$$

are indeed solutions of the effective Schrodinger equation describing two state kaon system:

$$i\hbar \frac{\partial |\psi(t)\rangle}{\partial t} = \mathcal{H}_{eff} |\psi(t)\rangle$$

3. Find the time dependent probability of the transition of a kaon into an anti-kaon particle:

$$P(\bar{K}^0, t) = |\langle \bar{K}^0 | K^0(t) \rangle|^2$$

4. Neutral meson P^0 and its antiparticle \bar{P}^0 decays to the same final state f . Calculate:
 - a) the decay rates

$$\Gamma_f = |\langle f | H | P^0(t) \rangle|^2 \text{ and } \bar{\Gamma}_f = |\langle f | H | \bar{P}^0(t) \rangle|^2$$

- b) the CP asymmetry of the form:

$$a_{CP}(t) = \frac{\Gamma_f - \bar{\Gamma}_f}{\Gamma_f + \bar{\Gamma}_f}$$

5. Show that CP asymmetry for the channel $B^0 \rightarrow J/\psi K_S$ (“golden channel”) can be used to extract unitary angle β . Start with the asymmetry:

$$a_{CP}(t) = \frac{\Gamma(B^0 \rightarrow J/\psi K_S) - \Gamma(\bar{B}^0 \rightarrow J/\psi K_S)}{\Gamma(B^0 \rightarrow J/\psi K_S) + \Gamma(\bar{B}^0 \rightarrow J/\psi K_S)}$$

6. Write the equation describing the direct CPV in charged B-meson decay, for example $B^0 \rightarrow K^+ \pi^-$.
7. Determine the sensitivity of CKM γ angle measurement in $B^0 \rightarrow D^0 K^{*0}$ decay.