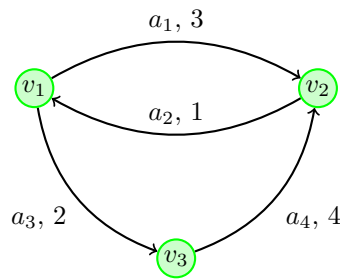


Graph	$G = (V, E)$
Vertices/nodes	$V = \{v_i : i = 1, \dots, 19\}$
Order	$ V = 19$
Edges/links	$E = \{e_j : j = 1, \dots, 28\}$ E.g., $e_{16} = \{v_{11}, v_{14}\}$
Size	$ E = 28$
Adjacency	E.g., vertices v_{11} and v_{14} are adjacent
Incidence	E.g., vertex v_{11} is incident with edge e_{16}
Vertex/nodal degree	E.g., $deg(v_9) = 4$
Handshaking theorem	E.g., $deg(v_1) = deg(v_3)$
Average degree	$E[deg] = \frac{1 \times 2 + 2 \times 5 + 3 \times 7 + 4 \times 2 + 5 \times 3}{19} = 2 \frac{ E }{ V } \approx 2.95$
Path	E.g., between v_7 and v_{14} : blue one $\langle v_7, v_{14} \rangle_{blue} = \langle v_7, v_9, v_{11}, v_{14} \rangle = \langle e_9, e_{14}, e_{16} \rangle$ and red one $\langle v_7, v_{14} \rangle_{red} = \langle v_7, v_{10}, v_{11}, v_{12}, v_{13}, v_{15}, v_{14} \rangle = \langle e_{10}, e_{15}, e_{17}, e_{18}, e_{19}, e_{20} \rangle$
Path length	E.g., $ \langle v_7, v_{14} \rangle_{red} = 6$
Distance	E.g., between vertices v_7 and v_{14} : $dist(v_7, v_{14}) = \min_k \{ \langle v_7, v_{14} \rangle_k \} = 3$
Diameter of a graph	$d(G) = \max_{i,j} dist(v_i, v_j) = \max_{i,j} \min_k \{ \langle v_i, v_j \rangle_k \} = dist(v_1, v_{19}) = 9$
Edge partition set	E.g., $\{e_4, e_5, e_{15}, e_{16}, e_{19}\}$
Cut	E.g., $\{e_4, e_5\}$
Bridge	E.g., e_3
Edge connectivity	$\lambda(G) = 1$
Vertex partition set	E.g., $\{v_1, v_5, v_6\}$
Vertex cut	E.g., $\{v_5, v_6\}$
Articulation point	E.g., v_7
Vertex connectivity	$\kappa(G) = 1$
Subgraphs	Full mesh, e.g., $K_3 = (\{v_{16}, v_{17}, v_{19}\}, \{e_{24}, e_{26}, e_{27}\})$ Cyclic, e.g., $C_4 = (\{v_7, v_8, v_{10}, v_{11}\}, \{e_8, e_{10}, e_{13}, e_{15}\})$ Linear, e.g., $P_3 = (\{v_2, v_4, v_5\}, \{e_3, e_4\})$ Full bipartite, e.g., $K_{2,3} = (\{v_8, v_{10}\} \cup \{v_7, v_9, v_{11}\}, \{e_8, e_{10}, e_{11}, e_{12}, e_{13}, e_{15}\})$
Spanning tree	E.g., $T = (V, \{e_1, e_2, e_3, e_4, e_5, e_6, e_8, e_{11}, e_{12}, e_{14}, e_{17}, e_{18}, e_{19}, e_{20}, e_{22}, e_{24}, e_{25}, e_{27}\})$
Adjacency matrix	E.g., for subgraph $(\{v_1, v_2, v_3, v_4\}, \{e_1, e_2, e_3\})$: $\mathbf{A} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 1 & 0 & 1 & 1 \\ 0 & 1 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}$
Incidence matrix	E.g., for subgraph $(\{v_1, v_2, v_3, v_4\}, \{e_1, e_2, e_3\})$: $\mathbf{B} = \begin{bmatrix} 1 & 0 & 0 \\ 1 & 1 & 1 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$

Digraph D



Weighted digraph
Arcs

$D = (V, A, w)$
 $A = \{a_i : i = 1, \dots, 4\}$
E.g., $a_1 = (v_1, v_2)$

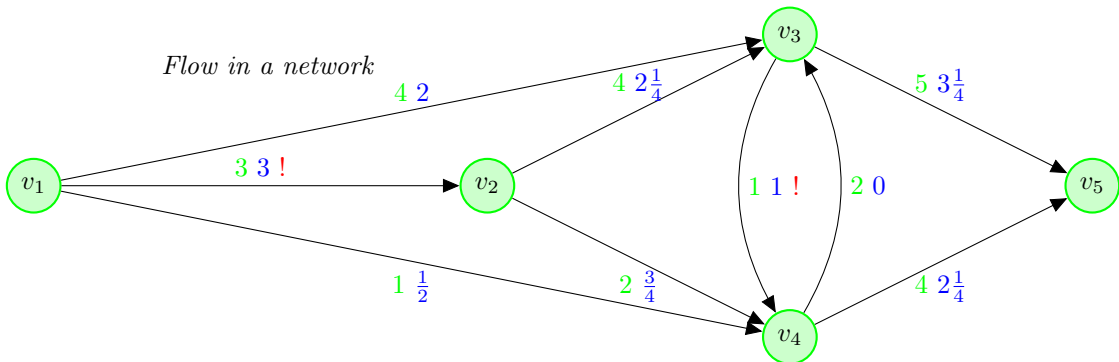
Incidence matrix of a digraph

$$\mathbf{B} = \begin{bmatrix} 1 & -1 & 1 & 0 \\ -1 & 1 & 0 & -1 \\ 0 & 0 & -1 & 1 \end{bmatrix}$$

Weight of an arc
Node strength

E.g., $w(a_1) = 3$
E.g., for v_1 equals 5

Flow in a network



Source
Sink/destination

v_1
 v_5

Capacity

E.g., $c(v_1, v_3) = 4$

Flow

Flow between v_1 and v_5 is equal to $5\frac{1}{2}$, since $f(v_3, v_5) + f(v_4, v_5) = 5\frac{1}{2}$

‘Nodal Kirchhoff’s theorem’
(flow conservation law)

E.g., for v_3 : $f(v_1, v_3) + f(v_2, v_3) + f(v_4, v_3) = f(v_3, v_4) + f(v_3, v_5)$

Saturated arc/link

E.g., (v_1, v_2) , since $f(v_1, v_2) = c(v_1, v_2)$