

There are the following JAVA classes implementing the multi-frontal direct solver algorithm for finite difference problem:

- *A.java*
- *A1.java*
- *A2.java*
- *AN.java*
- *Aroot.java*
- *BS.java*
- *E2.java*
- *Eroot.java*
- *Executor.java*
- *Main.java*
- *P1.java*
- *P2.java*
- *P3.java*
- *Production.java*
- *Vertex.java*

We have already implemented all the classes responsible for matrix transformations. We already have the *Executor* class constructing the elimination tree:

```
1 import java.util.concurrent.BrokenBarrierException;
2 import java.util.concurrent.CyclicBarrier;
3 class Executor extends Thread {
4     public synchronized void run() {
5         barrier barrier = new barrier(this);
6         Vertex S = new Vertex(null,null,null,''S'');
7         try {
8             //[(P1)]
9             CyclicBarrier barrier = new CyclicBarrier(1);
```

```

10     P1 p1 = new P1(S,barrier);
11     p1.start();
12     barrier.await();
13     //[(P2)1(P2)2]
14     barrier = new CyclicBarrier(2);
15     P2 p2a = new P2(p1.m_vertex.m_left,barrier);
16     P2 p2b = new P2(p1.m_vertex.m_right,barrier);
17     p2a.start();
18     p2b.start();
19     barrier.await();
20     //[(P2)3(P2)4(P3)5(P3)6]
21     barrier = new CyclicBarrier(4);
22     P2 p2c = new P2(p2a.m_vertex.m_left,barrier);
23     P2 p2d = new P2(p2a.m_vertex.m_right,barrier);
24     P3 p3a = new P3(p2b.m_vertex.m_left,barrier);
25     P3 p3b = new P3(p2b.m_vertex.m_right,barrier);
26     p2c.start();
27     p2d.start();
28     p3a.start();
29     p3b.start();
30     barrier.await();
31     //[(P3)1(P3)2(P3)3(P3)4]
32     barrier = new CyclicBarrier(2);
33     P3 p3c = new P3(p2c.m_vertex.m_left,barrier);
34     P3 p3d = new P3(p2c.m_vertex.m_right,barrier);
35     P3 p3e = new P3(p2d.m_vertex.m_left,barrier);
36     P3 p3f = new P3(p2d.m_vertex.m_right,barrier);
37     p3c.start();
38     p3d.start();
39     p3e.start();
40     p3f.start();
41     } catch (InterruptedException | BrokenBarrierException e) {
42         e.printStackTrace(); }
43     }
44 }
```

We can execute now graph grammar productions responsible for execution of the solver algorithm, see Figure 1

Please complete the *Executor* class by adding the graph grammar produc-

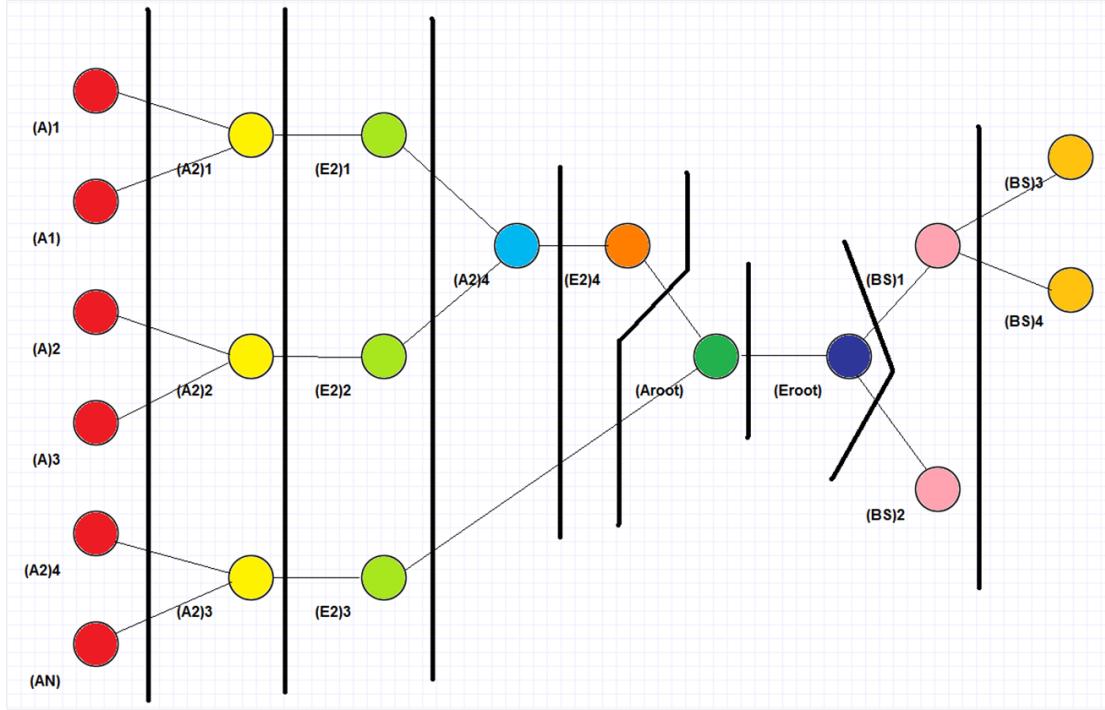


Figure 1: Graph of tasks responsible for execution of the solver algorithm.

tions responsible for solver execution.

Hint:

```

1  class Executor extends Thread {
2      public synchronized void run() {
3          // CONSTRUCTION OF ELIMINATION TREE
4          ...
5          // MULTI-FRONTAL SOLVER ALGORITHM
6          //[(A1)(A1)(A2)(A3)(A4)(AN)]
7          barrier = new CyclicBarrier(6);
8          A1 localMat1 = new A1(p3c.m_vertex, barrier);
9          A localMat2 = new A(p3d.m_vertex, barrier);
10         A localMat3 = new A(p3e.m_vertex, barrier);
11         A localMat4 = new A(p3f.m_vertex, barrier);
12         A localMat5 = new A(p3a.m_vertex, barrier);
13         AN localMat6 = new AN(p3b.m_vertex, barrier);
14         localMat1.start(); localMat2.start(); localMat3.start();

```

```
15     localMat4.start(); localMat5.start(); localMat6.start();
16     barrier.await();
17     //[(A2)1(A2)2(A2)3]
18     barrier = new CyclicBarrier(3);
19     A2 mergedMat1 = new A2(p2c.m_vertex, barrier);
20     A2 mergedMat2 = new A2(p2d.m_vertex, barrier);
21     A2 mergedMat3 = new A2(p2b.m_vertex, barrier);
22     mergedMat1.start(); mergedMat2.start(); mergedMat3.start();
23     barrier.await();
24     // PLEASE CONTINUE HERE .
25     ...
26 }
27 }
```

Please compile all the JAVA classes and run the solver.

Please print out the solution from the leaves of the elimination tree.