There are the following JAVA classes implementing the multi-frontal direct solver algorithm for time dependent problem:

- A.java
- A1.java
- *A2.java*
- AN.java
- Aroot.java
- BS.java
- E2.java
- Eroot.java
- Executor.java
- Main.java
- P1.java
- P2.java
- *P3.java*
- Production.java
- Vertex.java

We focus now on  $\alpha$ -scheme with respect to time mixed with finite element method with linear basis functions for space

We have already reimplemented all the classes responsible for generation of element matrices, as well as we have added the element diameter h, the time step dt, and the previous time step solution  $x_old$  to Vertex class.

We need now to update the Executor class so it works in a loop, for particular time steps:

```
class Executor extends Thread {
public synchronized void run() {
    // CONSTRUCTION OF ELIMINATION TREE
}
```

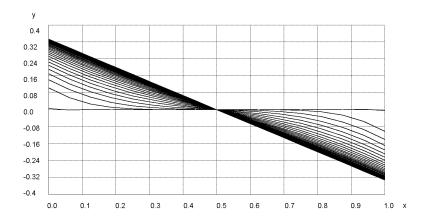


Figure 1: Exemplary plot with the solutions from particular time steps.

```
5
        N = \dots // Static number of intervals and time step
6
        Production.h = 1 / N;
7
        Production.dt = 0.001 / N;
8
        // x_old = 0 set by constructor
9
        // LOOP with respect to time steps
10
        for(step=1; step<1000; step++)</pre>
11
12
        // MULTI-FRONTAL SOLVER ALGORITHM
13
14
        // LOOP with respect to time steps
15
16
      }
17
    }
```

- 1. Please finish the implementation, compile and run the code.
- 2. Please extend the Executor class so it generates elimination trees of size  $2^k$  .
- 3. Please add a class responsible for plotting of the numerical solution, e.g., through interfacing with *gnuplot*. Please execute the non-stationary algorithm and generate the plot of the solutions from particular time steps, like the one presented in Figure 1.