

W poniższych zadaniach policzyć

$$\text{całki: } \int_C \vec{F} \cdot d\vec{r}$$

Zad. 1  $\vec{F}(x, y, z) = (y+z, x+z, x+y)$ ,

$$C = \{(x, y, z) : x = t, y = t^2, z = t^3, \text{ gdzie } 0 \leq t \leq 1\}$$

Zad. 2  $\vec{F}(x, y, z) = (z, x, y)$ ,

$$C = \{(x, y, z) : x = \sin t, y = 3 \sin t, z = \sin^2 t, 0 \leq t \leq \frac{\pi}{2}\}.$$

Zad. 3  $\vec{F}(x, y, z) = (x, y, z)$ ,

$$C = \{(x, y, z) : x = t^2, y = 4t + 1, z = t - 1, 1 \leq t \leq 4\}.$$

Zad. 4  $\vec{F}(x, y, z) = (yz, -xz, xy)$ ,

$$C = \{(x, y, z) : x = e^t, y = e^{3t}, z = e^{-t}, 0 \leq t \leq 1\}.$$

Zad. 5  $\vec{F}(x, y) = (x^2 + y^2, -x)$ ,

$$C = \{(x, y) : y = \sqrt{1 - x^2}, 0 \leq x \leq 1\}.$$

Zad. 6

$$\vec{F}(x, y) = (y^2 - 2xy, y^2 - 2xy)$$
,

$$C = \{(x, y) : y = 1 - |1 - x|, 0 \leq x \leq 2\}.$$

Zad. 7

$$\vec{F}(x, y, z) = (3x^2, 2xz - y, z)$$

$$C = \{(x, y, z) : y = \frac{1}{4}x^2, z = \frac{3}{8}x^3, 0 \leq x \leq 2\}.$$