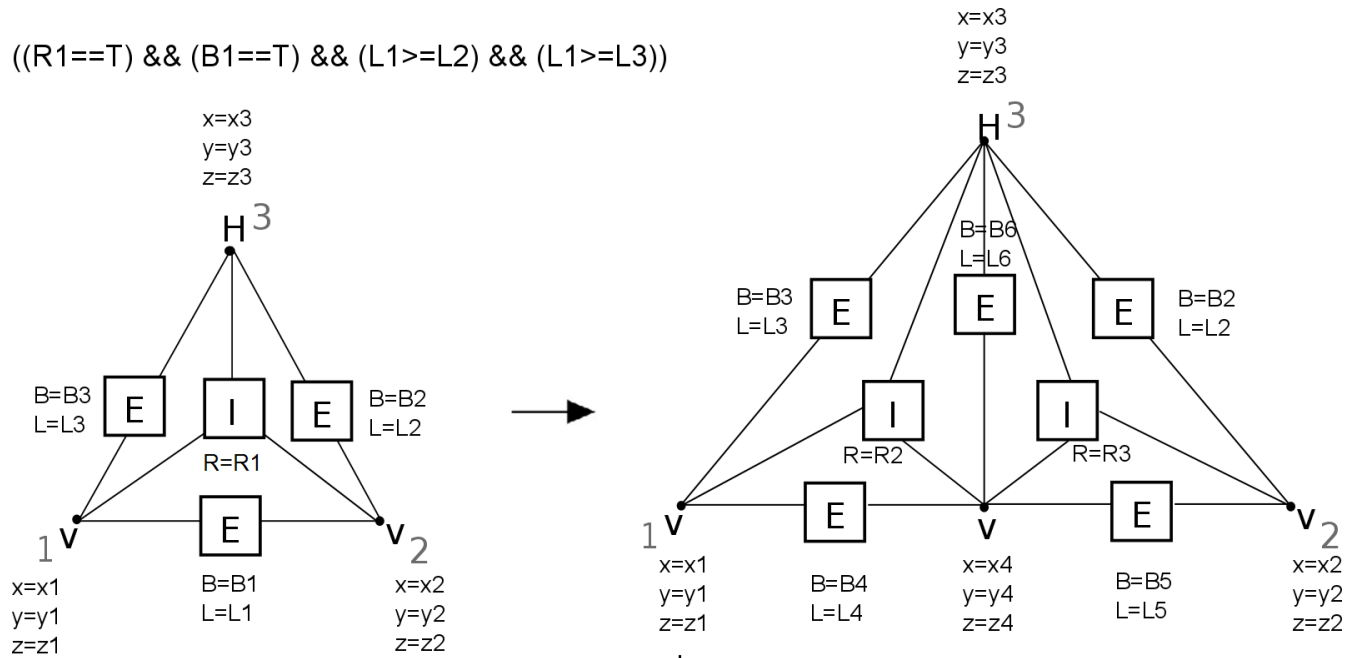


Graph transformations modeling terrain topography for CAD/CAE Systems
 Anna Paszynska & Maciej Paszynski & Krzysztof Podsiadlo (c)

1. Please implement graph transformation (P1)

$((R1==T) \ \&\& \ (B1==T) \ \&\& \ (L1 \geq L2) \ \&\& \ (L1 \geq L3))$

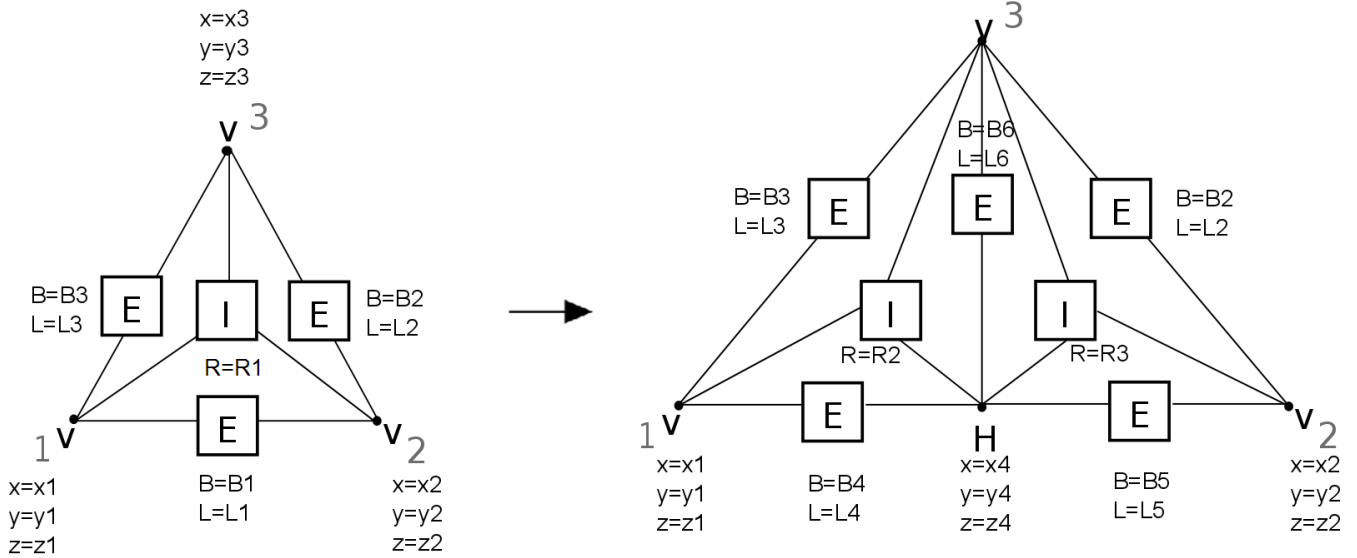


where:
 $L4=L1/2$
 $B4=B1$
 $L5=L1/2$
 $B5=B1$
 $x4=(x1+x2)/2$
 $y4=(y1+y2)/2$
 $z4=(z1+z2)/2$
 $L6=\text{sqrt}((x3-x4)^2+(y3-y4)^2+(z3-z4)^2)$
 $R2=F$
 $R3=F$
 $B6=F$

2. Please implement unit test for graph transformation described in 1, concerning rule (P1).

3. Please implement graph transformation (P2)

$((R1==T) \ \&\& \ (B1==F) \ \&\& \ (L1>=L2) \ \&\& \ (L1>=L3) \ \&\& \ !(\ (B2==T) \ \&\& \ L2==L1) \ || \ (B3==T) \ \&\& \ L3==L1))$

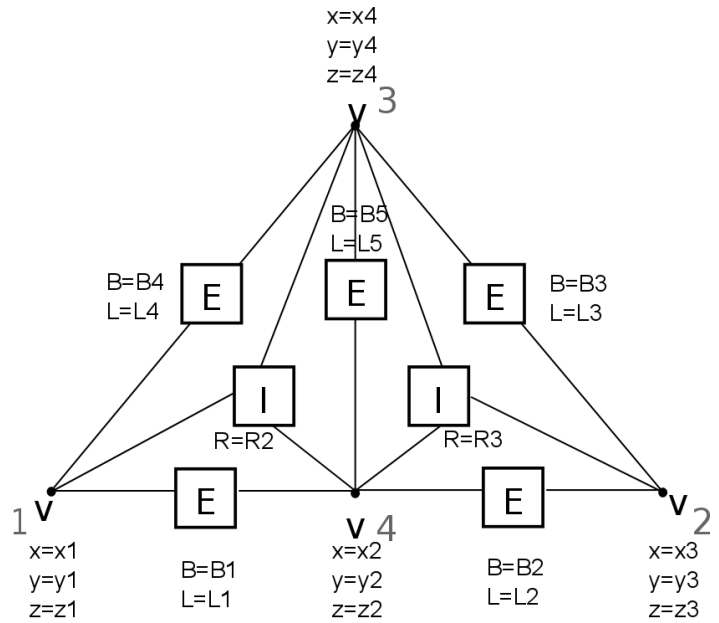
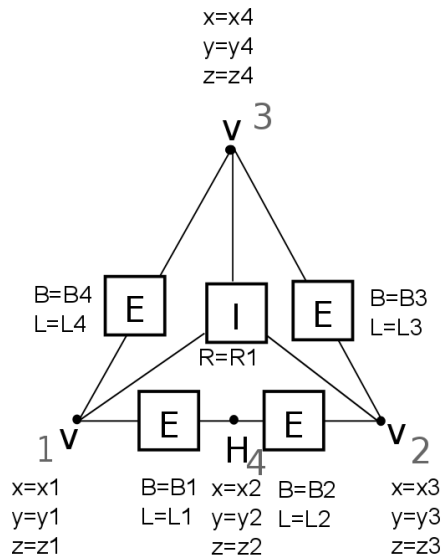


where:
 $L4=L1/2$
 $B4=B1$
 $L5=L1/2$
 $B5=B1$
 $x4=(x1+x2)/2$
 $y4=(y1+y2)/2$
 $z4=(z1+z2)/2$
 $L6=\text{sqrt}((x3-x4)^2+(y3-y4)^2+(z3-z4)^2)$
 $B6=F$
 $R2=F$
 $R3=F$

4. Please implement unit test for graph transformation described in 3, concerning rule (P2).

5. Please implement graph transformation (P3)

$((L1+L2) \geq L3) \ \&\& \ ((L1+L2) \geq L4)$



where:

$R_2 = F$

$R_3 = F$

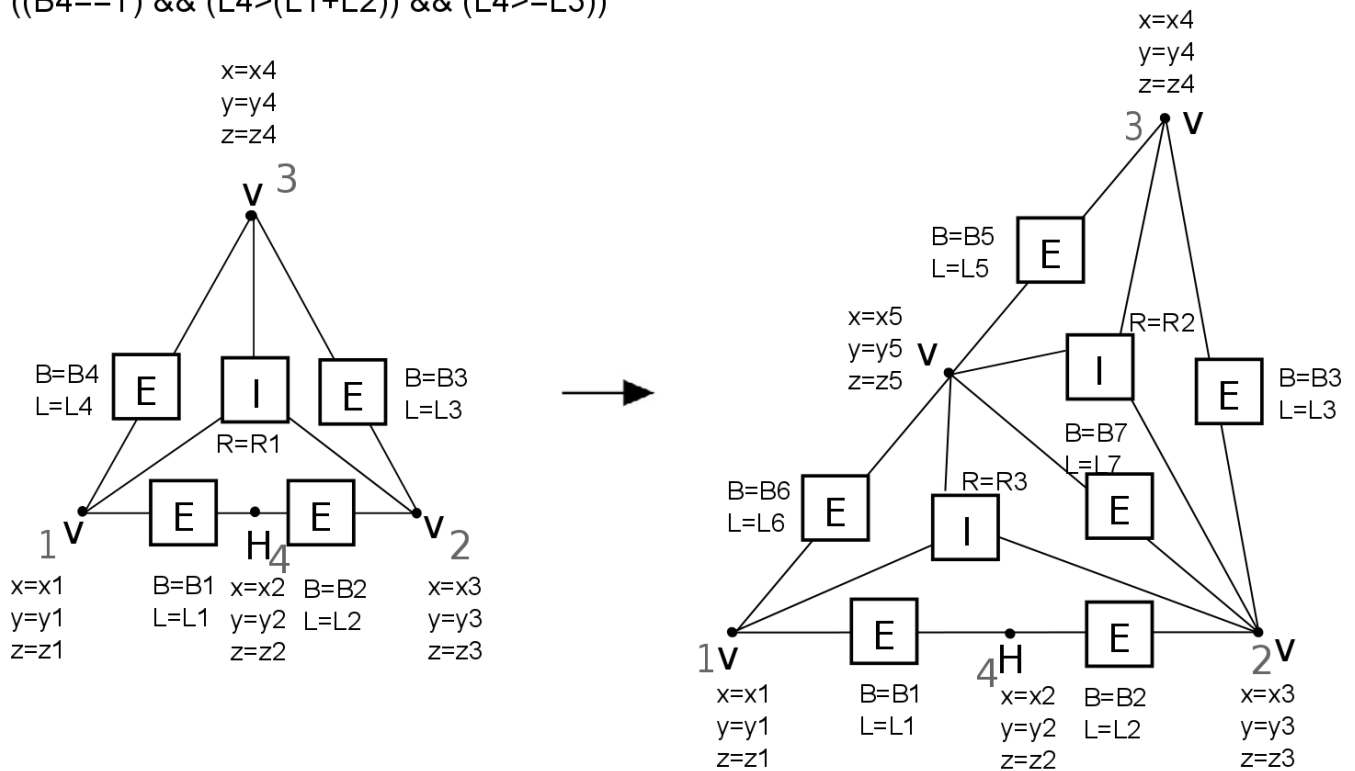
$L_6 = \sqrt{(x_2 - x_4)^2 + (y_2 - y_4)^2 + (z_2 - z_4)^2}$

$B_6 = F$

6. Please implement unit test for graph transformation described in 5, concerning rule (P3).

7. Please implement graph transformation (P4)

$((B4==T) \ \&\& \ (L4>(L1+L2)) \ \&\& \ (L4>=L3))$



where:

$L5=L4/2; B5=B4$

$L6=L4/2; B6=B4$

$x5=(x1+x4)/2$

$y5=(y1+y4)/2$

$z5=(z1+z4)/2$

$L7=\text{sqrt}((x3-x5)^2+(y3-y5)^2+(z3-z5)^2)$

$B7=F$

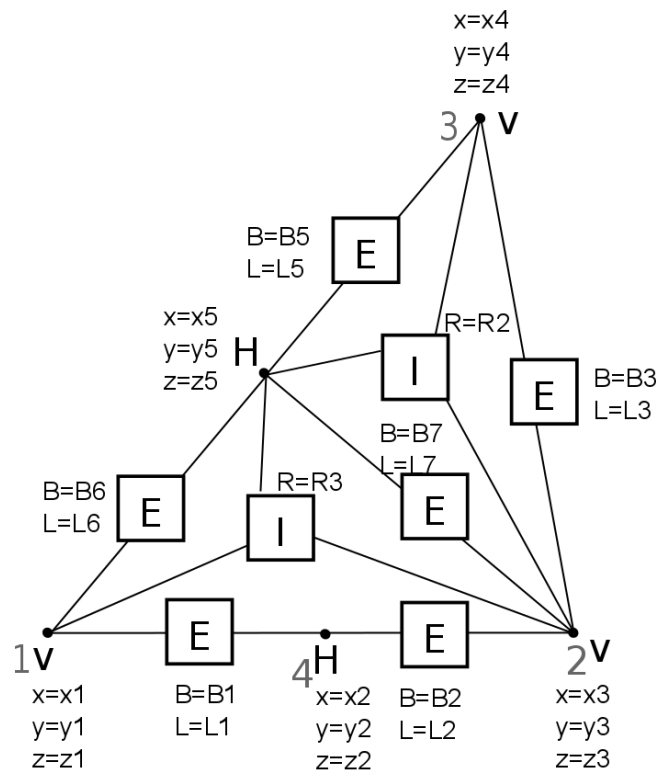
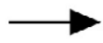
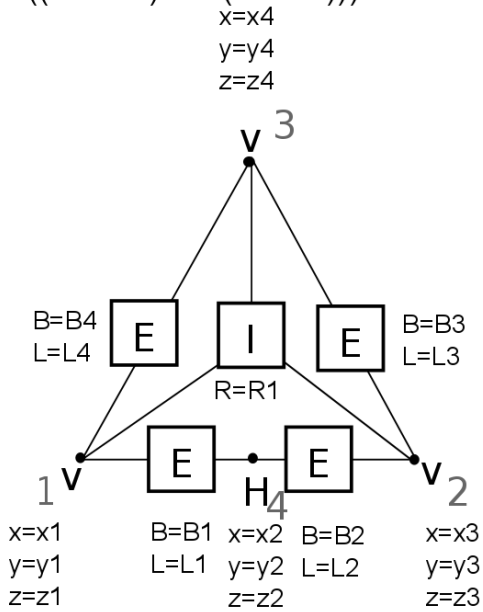
$R2=F$

$R3=F$

8. Please implement unit test for graph transformation described in 7, concerning rule (P4).

9. Please implement graph transformation (P5)

$((B4==F) \ \&\& \ (L4>(L1+L2)) \ \&\& \ (L4>=L3) \ \&\& \ !((B3==T) \ \&\& \ (L3=L4)))$



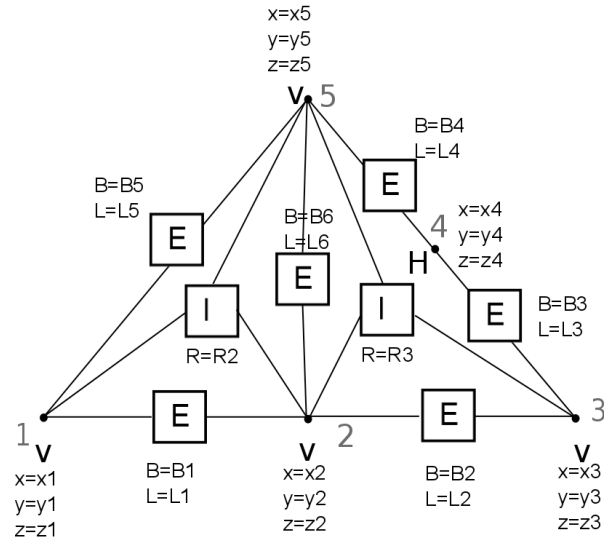
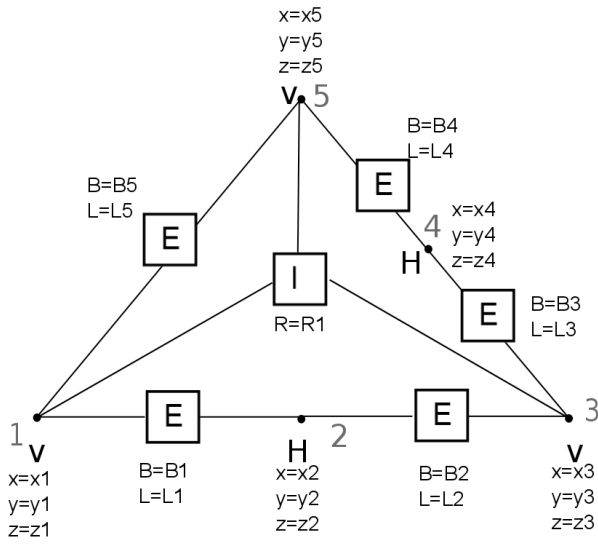
where:

- $L5=L4/2; \ B5=B4$
- $L6=L4/2; \ B6=B4$
- $x5=(x1+x4)/2$
- $y5=(y1+y4)/2$
- $z5=(z1+z4)/2$
- $L7=\sqrt{((x3-x5)^2+(y3-y5)^2+(z3-z5)^2)}$
- $B7=F$
- $R2=F$
- $R3=F$

10. Please implement unit test for graph transformation described in 9, concerning rule (P5).

11. Please implement graph transformation (P6)

$$((L1+L2) \geq (L3+L4)) \ \&\& \ ((L1+L2) \geq L5)$$



where:

R2=F

R3=F

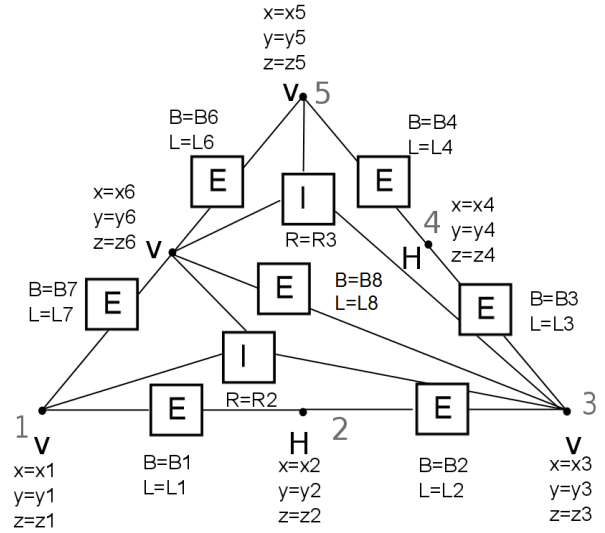
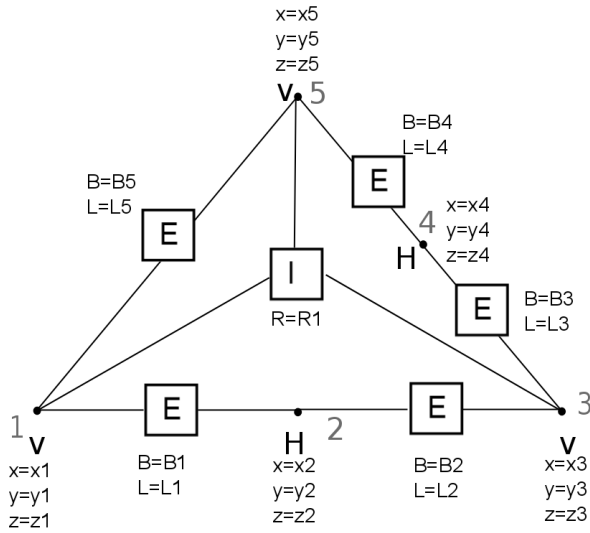
$L6 = \sqrt{(x2-x5)^2 + (y2-y5)^2 + (z2-z5)^2}$

B6=F

12. Please implement unit test for graph transformation described in 11, concerning rule (P6).

13. Please implement graph transformation (P7)

((B5==T) && (L5>(L1+L2)) && (L5>(L3+L4)))



where:

$$L6=L5/2; B6=B5$$

$$L7=L5/2; B7=B5$$

$$x6=(x1+x5)/2$$

$$y6=(y1+y5)/2$$

$$z6=(z1+z5)/2$$

$$L8=\sqrt{((x3-x6)^2+(y3-y6)^2+(z3-z6)^2)}$$

$$B8=F$$

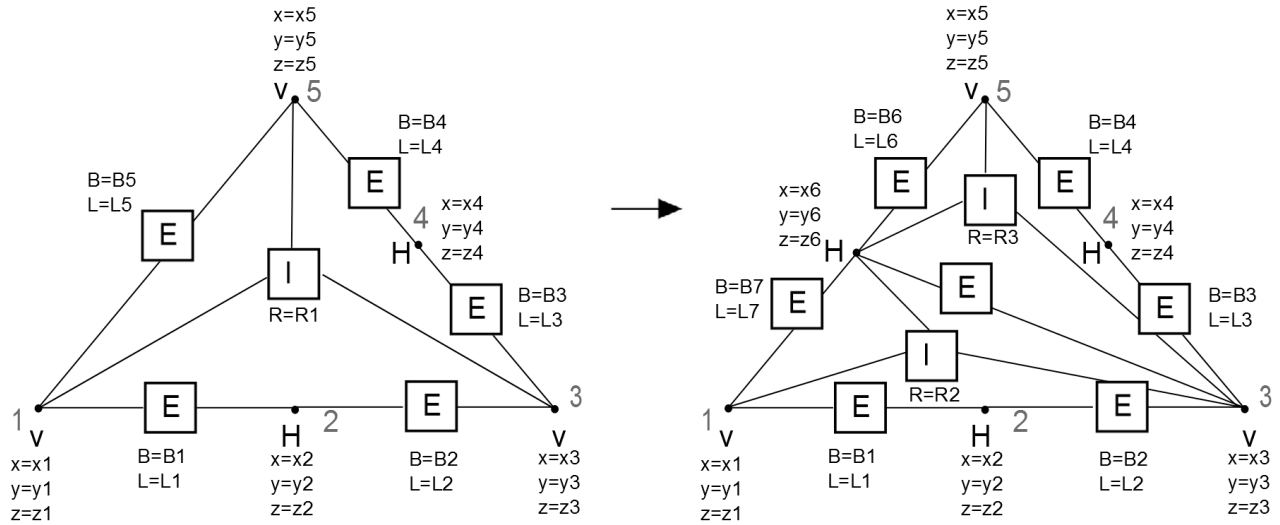
$$R2=F$$

$$R3=F$$

14. Please implement unit test for graph transformation described in 13, concerning rule (P7).

15. Please implement graph transformation (P8)

$((B5==F) \ \&\& \ (L5>(L1+L2)) \ \&\& \ (L5>(L3+L4)))$

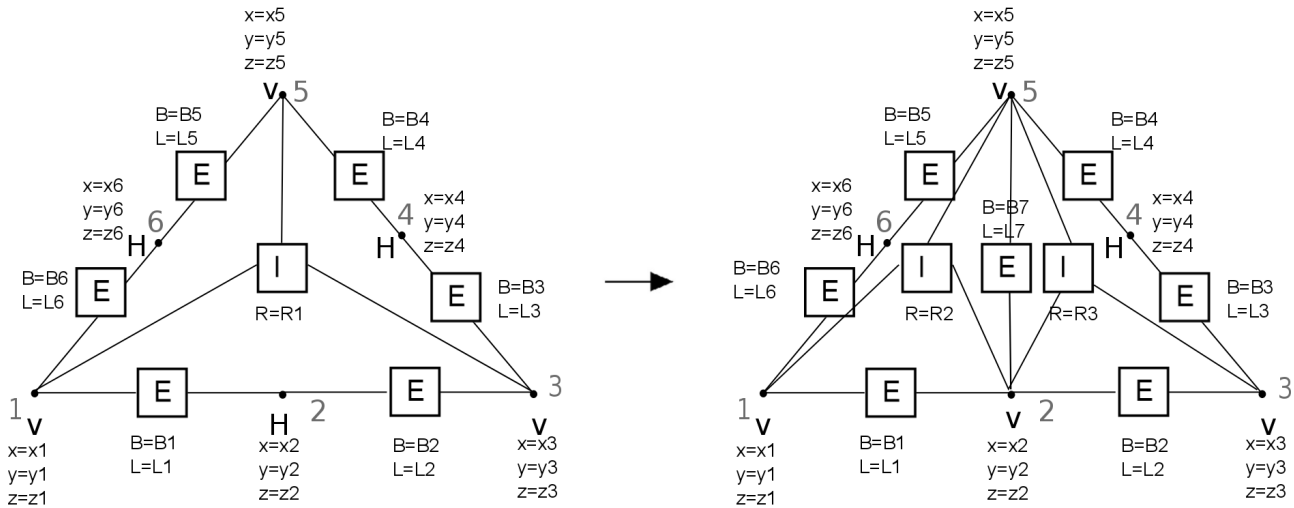


where:
 $L6=L5/2; B6=B5$
 $L7=L5/2; B7=B5$
 $x6=(x1+x5)/2$
 $y6=(y1+y5)/2$
 $z6=(z1+z5)/2$
 $L7=\sqrt{((x3-x6)^2+(y3-y6)^2+(z3-z6)^2)}$
 $B8=F$
 $R2=F$
 $R3=F$

16. Please implement unit test for graph transformation described in 15, concerning rule (P8).

17. Please implement graph transformation (P9)

$((L1+L2) \geq (L3+L4)) \ \&\& \ ((L1+L2) \geq (L5+L6))$



where:
 $B7 = F$
 $L7 = \sqrt{(x5-x2)^2 + (y5-y2)^2 + (z5-z2)^2}$

18. Please implement unit test for graph transformation described in 17, concerning rule (P9).

19. Please download, compile and run <https://github.com/Podsiadlo/terrain>

For example, for Europe

```
tergen -o out -Y -d Data/SRTM3 -x 100 -y 100 -z 100 -i 5 -j 5 -k 1 -N 68 -S 35 -E 50 -W -10
```

based on NASA database it generates files with terrain data.

-N -S range (-90,90) along the meridian, -W -E range (-180,180) along the equator

-i -j -k number of output files

-x, -y, -z number of terrain points, sorted from bottom to top layers, from W to E, from N to S, =0 if air, =1 if terrain

Data/SRTM3 NASA database directory (to be downloaded)

-o out name of the input file

Please generate data for Poland with 1 file and 3000 x 3000 x 3000 points (around 300 meters grid)

20. Procedure estimating the terrain approximation error for a given triangle

- Find all terrain points located in the triangle area
- Compute terrain points resulting from triangular approximation
- Compute sum of squares of differences between real terrain points and triangle approximation points
- Compute sum of squares of real terrain points located in the triangle area
- Divide c) by d)

21. Algorithm marking triangles for refinement

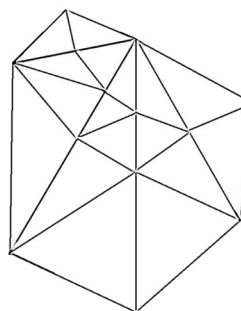
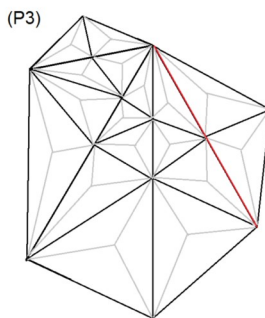
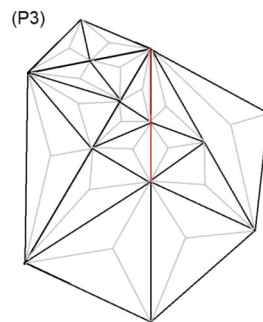
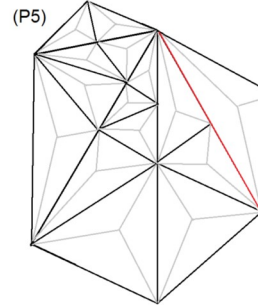
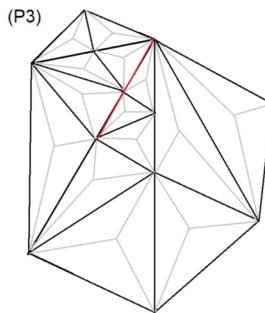
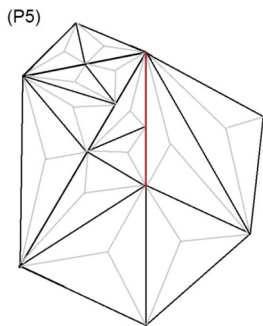
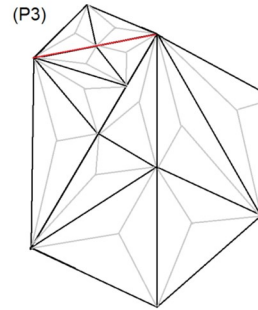
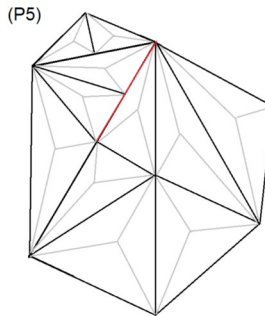
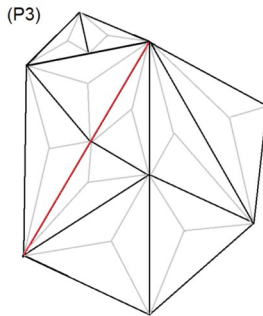
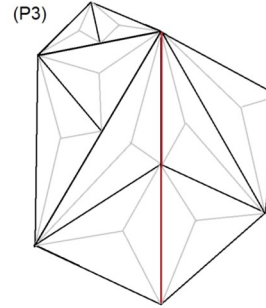
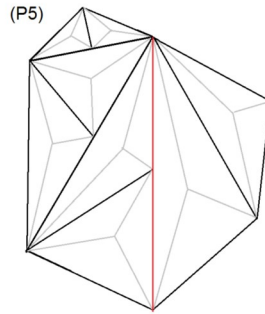
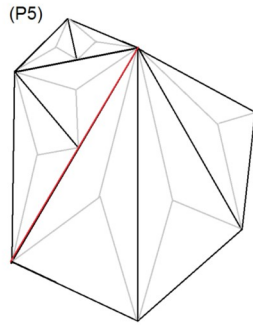
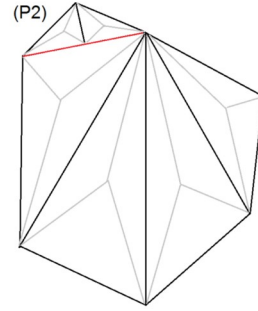
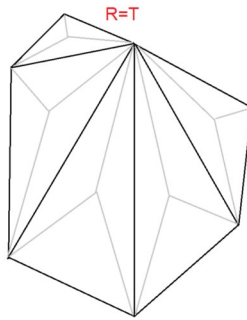
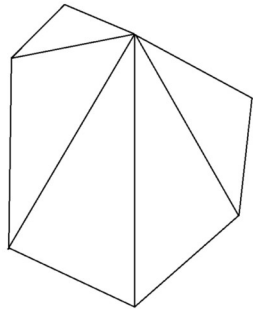
- a) Start from a mesh constructed from two triangles forming a rectangle, span over the terrain
- b) Loop over triangles T
 - b.1) Estimate approximation error over T
 - b.2) If error is larger than given epsilon, mark triangle for refinement

22. Please implement reasonable integration test for algorithm from point 21

23. Algorithm for mesh adaptation

- a) Execute all possible graph transformations P1
- b) Execute all possible graph transformations P2
- c) Execute all possible graph transformations P3
- d) Execute all possible graph transformations P4
- e) Execute all possible graph transformations P5
- f) Execute all possible graph transformations P6
- g) Execute all possible graph transformations P7
- h) Execute all possible graph transformations P8
- i) Execute all possible graph transformations P9
- j) If no graph transformations P3,P4,P5,P6,P7,P8,P9 were executed in points c)-i) then STOP
- k) Go to c)

24. Please implement integration test for algorithm from point 23, using the sketch below



25. Proszę stworzyć następującą siatkę reprezentowaną przez naszą strukturę grafu
Proszę uruchomić algorytm z punktu 23 na tej siatce, I zwizualizować zmiany (adaptacje siatki)

