

# Informatyka

E-podręczniki

Moduły

## MATLAB implementation of the adaptive algorithm for the bitmap projection problem

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In this module, we present the MATLAB code that computes the L2 bitmap projection using the adaptive finite element method. In particular, this code has an implementation of the h-adaptation algorithm in MATLAB. Code execution is also possible in the free Octave environment. The code is presented below

```
% This is a implementation of h-adaptive bitmap projection.
%
% How to use
%
% bitmap(filename as a string, number of elements along x axis, , number of elements along y axis, maximum error)
%
% Examples
%
% bitmap("mp.JPG", 10,10,0.1,3,false)
% bitmap("basket.JPG", 20,20,0.5,1,true)
function bitmap_h(filename,elementsx,elementsy,maxerror,max_refinement_level,color_edges_black)

% read image from file
```

```
XX = imread(filename);

% extract red, green and blue components
RR = XX(:,:,1);
GG = XX(:,:,2);
BB = XX(:,:,3);

% read size of image
ix = size(XX,1);
iy = size(XX,2);

% global count of vertexes
total_vertexes = 0;
% global count of elements
total_elements = 0;

% element structure contains:
% * vertices - organized as followed:
%
% ul - ur
% |   |
% dl - dr
%
% ul - up-left
% ur - up-right
% dl - down-left
% dr - down-right
%
```

```

% * neighbours (elements) ogranized as followed
% there can be up to two neighbours on each edge
% default neighours (if there is one neighbour) are:
% eul, elu, eru, edl
%
%      eul eur
%
%      ___  ___
% elu |   |   | eru
%     |   |   |
% eld |___|___| erd
%      edl edr
%
% eul - element-up-left
% eur - element-up-rgiht
% elu - element-left-up
% eld - element-left-down
% eru - element-right-up
% erd - element-right-down
% edl - element-down-left
% edr - element-down-right
%
% * active - we don't delete inactive elements, rather tag them as inactive
% * index - index of element in global elements table
%
elements = struct('dl',{},'ul',{},'dr',{},'ur',{},'active',{},'elu',{},'eld',{},'edl',{},'edr',{},'eul',{
%
% vertex data structure contains
% * x and y coordinates

```

```
% * r,g,b - red, green and blue components
% * index - index of vertex in global vertexes table
% * real - false if vertex is hanging node and has interpolated r,g,b components
%
vertexes = struct('x',{},'y',{},'r',{},'g',{},'b',{},'index',{},'real',{});

% initialize unbroken mesh
init_mesh();

redo_error_test = true;
refinement_level = 0;

% repeat until we match maximum local estimation error or maximum refinement level
while (redo_error_test && (refinement_level < max_refinement_level))
    redo_error_test = false;
% loop through elements
    for i=1:total_elements
% check only active elements
        if (elements(i).active)
% estimate relative interpolation error in red, green and blue components
            [rr,gg,bb] = estimate_error(i);
% if any of the errors is higher than our maximum -> break element and repeat entire loop
            if ((rr >= maxerror) || (gg >= maxerror) || (bb >= maxerror))
                redo_error_test = true;
                break_element(i);
            end
        end
    end
end
```

```
refinemenet_level = refinemenet_level + 1;
end

% interpolate all active elements - recreate bitmap red green and blue compoments
for i=1:total_elements
    if (elements(i).active)
        interpolate_elem(i,color_edges_black);
    end
end

% recreate bitmap from red, green and blue compoments
RGB=XX;
RGB(:,:,1) = RR;
RGB(:,:,2) = GG;
RGB(:,:,3) = BB;

% display image
imshow(RGB);

% create vertex (non hanging node)
function index=create_vertex(x,y)
    vert.x = x;
    vert.y = y;
    vert.r = RR(x,y);
    vert.g = GG(x,y);
    vert.b = BB(x,y);
    total_vertexes = total_vertexes + 1;
```

```
vert.index = total_vertexes;  
vert.real = true;  
vertexes(total_vertexes) = vert;  
index = total_vertexes;  
end
```

```
% create vertex (hanging node)
```

```
function index=create_vertex_rgb(x,y,r,g,b)  
vert.x = x;  
vert.y = y;  
vert.r = r;  
vert.g = g;  
vert.b = b;  
total_vertexes = total_vertexes + 1;  
vert.index = total_vertexes;  
vert.real = false;  
vertexes(total_vertexes) = vert;  
index = total_vertexes;  
end
```

```
% update vertex - when hanging node becomes non-hanging node
```

```
function vert_update(index)  
vert = vertexes(index);  
vert.r = RR(vert.x,vert.y);  
vert.g = GG(vert.x,vert.y);  
vert.b = BB(vert.x,vert.y);
```

```
vert.real = true;
vertexas(index) = vert;
end

% create initial element
function element=create_element(v1,v2,v3,v4)
    element.dl = v1;
    element.ul = v2;
    element.dr = v3;
    element.ur = v4;

    element.active = true;

% set all neighbours to null
    element.elu = 0;
    element.eld = 0;
    element.edl = 0;
    element.edr = 0;
    element.eul = 0;
    element.eur = 0;
    element.eul = 0;
    element.eru = 0;
    element.end = 0;

    total_elements = total_elements + 1;
    element.index = total_elements;
end
```

```
% initialize mesh
function init_mesh()
%
% vertexes mapping
%
% v2 -> ul
% v4 -> ur
% v1 -> dl
% v3 -> dr
%
elem_width = floor(ix / elementsx);
elem_hight = floor(iy / elementsy);

x = 0;
y = 0;

% create all vertexes
for i=0:elementsy-1
    for j=0:elementsx-1
        vertex = create_vertex(x+j*elem_width+1,y+1);
    end
    vertex = create_vertex(ix,y+1);
    y = y + elem_hight;
end
for j=0:elementsx-1
    vertex = create_vertex(x+j*elem_width+1,iy);
```



```
end
vertex = create_vertex(ix,iy);

% create all elements
for i=1:elementsy
    for j=1:elementsx
        v1 = (i-1)*elementsy+j + i-1;
        v3 = v1+1;
        v2 = i*elementsy+j+1 + i-1;
        v4 = v2+1;
        element = create_element(v1,v2,v3,v4);
        index = element.index;
% set neighbours for each element
        if(j~=1)
            element.elu = index-1;
        end
        if(j~=elementsx)
            element.eru = index+1;
        end
        if(i~=1)
            element.edl = index-elementsx;
        end
        if(i~=elementsy)
            element.eul = index+elementsx;
        end
        elements(index) = element;
    end
end
end
```

end

```
% interpolate r,g,b components for hanging node
% v1 and v2 are vertexes of given element on edges of broken edge
% v3 is interpolated vertex between v1 and v2
function v3=interpolate_rgb(v1,v2,element)
    elem = elements(element);
    width = vertexes(elem.dr).x - vertexes(elem.dl).x;
    hight = vertexes(elem.ul).y - vertexes(elem.dl).y;
    vert1 = vertexes(v1);
    vert2 = vertexes(v2);

    vert3.x = (vert1.x + vert2.x) /2;
    vert3.y = (vert1.y + vert2.y) /2;
    vert3.x = floor(vert3.x);
    vert3.y = floor(vert3.y);

    xx = vert3.x - vertexes(elem.dl).x;
    yy = vert3.y - vertexes(elem.dl).y;
    [r,g,b] = inpoint(xx,yy,width,hight,elem);

    vert3.r = r;
    vert3.g = g;
    vert3.b = b;
    vert3.real = false;
```

```
total_vertexes = total_vertexes + 1;
vert3.index = total_vertexes;
v3 = total_vertexes;
vertexes(v3) = vert3;
end

% interpolate r,g,b components of a element
function interpolate_elem(element,color_edges_black)
    elem = elements(element);
    width = vertexes(elem.dr).x - vertexes(elem.dl).x;
    hight = vertexes(elem.ul).y - vertexes(elem.dl).y;
    width = abs(width);
    hight = abs(hight);
    dlx = vertexes(elem.dl).x;
    dly = vertexes(elem.dl).y;

    for xx=0:width
        for yy=0:hight
            [r,g,b] = inpoint(xx,yy,width,hight,elem);
            RR(dlx+xx,dly+yy) = r;
            GG(dlx+xx,dly+yy) = g;
            BB(dlx+xx,dly+yy) = b;
        end
    end

    % create black edges on element if requested
    if (color_edges_black)
```

```
for xx=0:width
    RR(dlx+xx,dly) = 0;
    GG(dlx+xx,dly) = 0;
    BB(dlx+xx,dly) = 0;

    RR(dlx+xx,dly+hight) = 0;
    GG(dlx+xx,dly+hight) = 0;
    BB(dlx+xx,dly+hight) = 0;
end

for yy=0:hight
    RR(dlx,dly+yy) = 0;
    GG(dlx,dly+yy) = 0;
    BB(dlx,dly+yy) = 0;

    RR(dlx+width,dly+yy) = 0;
    GG(dlx+width,dly+yy) = 0;
    BB(dlx+width,dly+yy) = 0;
end
end
end

% computes r,g,b components of element in given point
function [r,g,b]=inpoint(xx,yy,width,hight,elem)
    f1 = fi1(xx,yy);
    f2 = fi2(xx,yy);
    f3 = fi3(xx,yy);
```

```
f4 = fi4(xx,yy);

r = vertexes(elem.dl).r * f1;
r = r + vertexes(elem.ul).r * f2;
r = r + vertexes(elem.dr).r * f3;
r = r + vertexes(elem.ur).r * f4;
r = floor(r);

g = vertexes(elem.dl).g * f1;
g = g + vertexes(elem.ul).g * f2;
g = g + vertexes(elem.dr).g * f3;
g = g + vertexes(elem.ur).g * f4;
g = floor(g);

b = vertexes(elem.dl).b * f1;
b = b + vertexes(elem.ul).b * f2;
b = b + vertexes(elem.dr).b * f3;
b = b + vertexes(elem.ur).b * f4;
b = floor(b);

% basis functions defined over element
function ret=fi1(xx,yy)
    x = xx/width;
    y = yy/hight;
    ret = (1-x) * (1-y);
end

function ret=fi2(xx,yy)
```

```
x = xx/width;
y = yy/hight;
ret = (1-x) * y;
end

function ret=fi3(xx,yy)
    x = xx/width;
    y = yy/hight;
    ret = x * (1-y);
end

function ret=fi4(xx,yy)
    x = xx/width;
    y = yy/hight;
    ret = x * y;
end
end

% if neighbour is already bigger than element that we try to break - we should break it as well
function break_neighbours(index)
    element = elements(index);

    check_left();
    check_right();
    check_up();
    check_down();
```

```
function check_left()
% no neighbours on the left
    if (element.elu == 0)
        return;
    end
% two neighbours on the left
    if(element.eld ~= 0)
        return;
    end
% only one neighbour on the left
    left = elements(element.elu);
    if (left.erd ~= 0)
% neighbour on the left has two neighbours on the right
        break_element(element.elu);
    end
end

function check_right()
% no neighbours on the right
    if (element.eru == 0)
        return;
    end
% two neighbours on the right
    if (element.erd ~= 0)
        return;
    end
% only one neighbour on the right
```

```
    right = elements(element.eru);
    if (right.eld ~= 0)
% neighbour on the right has two neighbours on the left
        break_element(element.eru);
    end
end

function check_up()
% no neighbours on the top
    if (element.eul == 0)
        return;
    end
% two neighbours on the top
    if (element.eur ~= 0)
        return;
    end
% only one neighbour on the top
    up = elements(element.eul);
    if (up.edr ~= 0)
% neighbour on the top has two neighbours on the bottom
        break_element(element.eul);
    end
end

function check_down()
% no neighbours on the bottom
    if (element.edl == 0)
        return;
```



```

    end
% two neighbours on the bottom
    if (element.edr ~= 0)
        return;
    end
% only one neighbour on the bottom
    down = elements(element.ed1);
    if (down.eur ~= 0)
% neighbour on the bottom has two neighbours on the top
        break_element(element.ed1);
    end
end
end
end

```

```

% breaking element

```

```

function break_element(index)

```

```

    element = elements(index);
    if (~element.active)
        disp('error!!!');
    end
    break_neighbours(index);
    element = elements(index);
% vertexes of element are organized as followed
%
% u1 - ur
% |   |

```

```
% dl - dr
%
% they are mapped to local vertices
%
% v2 - v4
% | e |
% v1 - v3
%
%
% after breaking element vertices and new elements are organized as followed
%
% v2 - v9 - v4
% | e2 | e4 |
% v6 - v7 - v8
% | e1 | e3 |
% v1 - v5 - v3
%
%
% e -> e2 e4
%      e1 e3
%
%
v1 = element.dl;
v2 = element.ul;
v3 = element.dr;
v4 = element.ur;

v5=0;
```

```
v6=0;
v7=0;
v8=0;
v9=0;

% if we have two neighbours left
if (element.eld ~= 0)
    eld = elements(element.eld);
    v6 = eld.ur;
    vert_update(v6);
% if we have unbroken neighbour left
else
    v6 = interpolate_rgb(v1,v2,index);
end
if (element.elu == 0)
    vert_update(v6);
end

% if we have two neighbours right
if (element.erd ~= 0)
    erd = elements(element.erd);
    v8 = erd.ul;
    vert_update(v8);
% if we have unbroken neighbour right
else
    v8 = interpolate_rgb(v3,v4,index);
end
if (element.eru == 0)
```

```
    vert_update(v8);
end

% if we have two neighbours up
if (element.eur ~= 0)
    eur = elements(element.eur);
    v9 = eur.dl;
    vert_update(v9)
% if we have unbroken neighbour up
else
    v9 = interpolate_rgb(v2,v4,index);
end
if (element.eul == 0)
    vert_update(v9);
end

% if we have two neighbours down
if (element.edr ~= 0)
    edr = elements(element.edr);
    v5 = edr.ul;
    vert_update(v5);
% if we have unbroken neighbour down
else
    v5 = interpolate_rgb(v1,v3,index);
end
if (element.edl == 0)
    vert_update(v5);
end
```

```
x = vertexes(v5).x;
y = vertexes(v6).y;

v7 = create_vertex(x,y);

element.active = false;
elements(element.index) = element;

e1 = create_element(v1,v6,v5,v7);
e2 = create_element(v6,v2,v7,v9);
e3 = create_element(v5,v7,v3,v8);
e4 = create_element(v7,v9,v8,v4);

% set neighbours between new elements
e1.eru = e3.index;
e1.eul = e2.index;
e2.edl = e1.index;
e2.eru = e4.index;
e3.elu = e1.index;
e3.eul = e4.index;
e4.elu = e2.index;
e4.edl = e3.index;

% set neighbours between new and old elements
e1.edl = element.edl;
if (element.edl ~= 0)
    edl = elements(element.edl);
```

```
    ed1.eul = e1.index;
    elements(ed1.index) = ed1;
end
if (element.edr ~= 0)
    e3.ed1 = element.edr;
    edr = elements(element.edr);
    edr.eul = e3.index;
    elements(edr.index) = edr;
else
    e3.ed1 = element.ed1;
    if (element.ed1 ~= 0)
        ed1 = elements(element.ed1);
        ed1.eur = e3.index;
        elements(ed1.index) = ed1;
    end
end

e2.elu = element.elu;
if (element.elu ~= 0)
    elu = elements(element.elu);
    elu.eru = e2.index;
    elements(elu.index) = elu;
end
if (element.eld ~= 0)
    e1.elu = element.eld;
    eld = elements(element.eld);
    eld.eru = e1.index;
    elements(eld.index) = eld;
```

```
else
    e1.elu = element.elu;
    if (element.elu ~= 0)
        elu = elements(element.elu);
        elu.erd = e1.index;
        elements(elu.index) = elu;
    end
end

e2.eul = element.eul;
if (element.eul ~= 0)
    eul = elements(element.eul);
    eul.edl = e2.index;
    elements(eul.index) = eul;
end

if (element.eur ~= 0)
    e4.eul = element.eur;
    eur = elements(element.eur);
    eur.edl = e4.index;
    elements(eur.index) = eur;
else
    e4.eul = element.eul;
    if (element.eul ~= 0)
        eul = elements(element.eul);
        eul.edr = e4.index;
        elements(eul.index) = eul;
    end
end
end
```

```
e4.eru = element.eru;
if (element.eru ~= 0)
    eru = elements(element.eru);
    eru.elu = e4.index;
    elements(eru.index) = eru;
end
if (element.erd ~= 0)
    e3.eru = element.erd;
    erd = elements(element.erd);
    erd.elu = e3.index;
    elements(erd.index) = erd;
else
    e3.eru = element.eru;
    if (element.eru ~= 0)
        eru = elements(element.eru);
        eru.eld = e3.index;
        elements(eru.index) = eru;
    end
end

elements(e4.index) = e4;
elements(e3.index) = e3;
elements(e2.index) = e2;
elements(e1.index) = e1;
end
```



```
% estimate relative error of interpolation over given element
function [error_r,error_g,error_b]=estimate_error(index)
    element = elements(index);
    dl = element.dl;
    ul = element.ul;
    dr = element.dr;
    ur = element.ur;

    x1 = vertexes(dl).x;
    yd = vertexes(dl).y;
    xr = vertexes(ur).x;
    yu = vertexes(ur).y;

    elementWidth = xr - x1;
    elementHeight = yu - yd;

% interpolate using L2 norm and Gaussian quadrature rule
x1 = elementWidth/2.0 - elementWidth / (sqrt(3.0) * 2.0);
x2 = elementWidth/2.0 + elementWidth / (sqrt(3.0) * 2.0);
y1 = elementHeight/2.0 - elementHeight / (sqrt(3.0) * 2.0);
y2 = elementHeight/2.0 + elementHeight / (sqrt(3.0) * 2.0);

x1 = floor(x1);
x2 = floor(x2);
y1 = floor(y1);
y2 = floor(y2);

[r1,g1,b1]=inpoint(x1,y1,elementWidth,elementHeight,element);
```

```
[r2,g2,b2]=inpoint(x1,y2,elementWidth,elementHeight,element);  
[r3,g3,b3]=inpoint(x2,y1,elementWidth,elementHeight,element);  
[r4,g4,b4]=inpoint(x2,y2,elementWidth,elementHeight,element);
```

```
r1 = r1 - RR(x1+x1,y1+yd);  
g1 = g1 - GG(x1+x1,y1+yd);  
b1 = b1 - BB(x1+x1,y1+yd);
```

```
r2 = r2 - RR(x1+x1,y2+yd);  
g2 = g2 - GG(x1+x1,y2+yd);  
b2 = b2 - BB(x1+x1,y2+yd);
```

```
r3 = r3 - RR(x2+x1,y1+yd);  
g3 = g3 - GG(x2+x1,y1+yd);  
b3 = b3 - BB(x2+x1,y1+yd);
```

```
r4 = r4 - RR(x2+x1,y2+yd);  
g4 = g4 - GG(x2+x1,y2+yd);  
b4 = b4 - BB(x2+x1,y2+yd);
```

```
error_r = r1*r1 + r2*r2 + r3*r3 + r4*r4;  
error_g = g1*g1 + g2*g2 + g3*g3 + g4*g4;  
error_b = b1*b1 + b2*b2 + b3*b3 + b4*b4;
```

```
error_r = double(error_r);  
error_g = double(error_g);  
error_b = double(error_b);
```

```
error_r = sqrt(error_r) * 100.0 / (255.0 * 2.0);  
error_g = sqrt(error_g) * 100.0 / (255.0 * 2.0);  
error_b = sqrt(error_b) * 100.0 / (255.0 * 2.0);  
end
```

```
end
```

Listing 1 ([Pobierz](#)): Adaptacyjna projekcja bitmapy

In order to run the codes, we save them in the Octave working directory.

We set the variables with the path to the input file in tif format

```
filename = ' C : \Users\Maciej\Dropbox\bitmapa.tif'
```

then we give the number of mesh elements in the x and y directions, and the degrees of B-spline in these directions

```
elementsx = 4, elementsy = 4 are the size of the initial grid.
```

We enter the maximum approximation error

```
maxerror = 0.5,
```

the maximum number of adaptation iterations *maxlevel* = 4

and indicate whether the mesh edges are to be drawn

```
edges = 1.
```

Then we start the first procedure

```
bitmap_h(filename, elementsx, elementsy, maxerror, maxlevel, edges).
```

The code after executing the adaptation sequence draws the bitmap in the open window.

---

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